

INSTRUCTIONS

1. The quiz contains multiple choice questions that must be answered in the orange code sheet we have provided you with.
2. To select an answer, all you need to do is mark in the orange code sheet, **filling the rectangle over which the selected answer is located appropriately**. Please make sure you know the answer you wish to mark before doing it. Even though you can always erase your mark if you have used a pencil (number 2 or similar), any mark that has not been completely erased could be read by the machine. Therefore, we advice you to first mark your selected answers in the exam and to use only the last ten minutes or so from the time assigned to the multiple choice questions part of the exam to copy them into the code sheet.
3. In the multiple choice questions part of the exam there is always **only one correct answer** for every question. Every question correctly answered is worth 1 point, while each question incorrectly answered will not penalize your grade at all. Questions that have not been answered do not penalize your grade in any form.
4. The quiz has four numbered sheets, going from 0.1 to 0.4. Please make sure that you have all sheets and contact your professor if this is not the case. There are different exam types. This exam is of type 0. Mark a 0 in the column labelled with I in your code sheet, just as it is illustrated in the example.
5. The maximum final grade is 14 points. **You will need to obtain 10 points to pass this quiz.**
7. Please fill in your personal information in the appropriate places in the code sheet.

Example:

12545 PEREZ, Ernesto

Exam type 0 Resit

CUESTION	NUMERO DEL ALUMNO
ENSEÑANZA	
OFICIAL	LIBRE
□	□
Observaciones	

D.N.I. / N.A.N.									
□	□	□	□	□	□	□	□	□	□
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗	⊗

NUMERO / ZENBAKIA				
□	□	□	□	□
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗	⊗

I	II	III	IV
□	□	□	□
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗
⊗	⊗	⊗	⊗

MULTIPLE CHOICE QUESTIONS (Time: 45 minutes)

1. FREE-QUESTION. The capital of Spain is:

- (A) Paris (B) Sebastopol (C) Madrid (D) London (E) Pekin

Questions 2 to 4 refer to the following exercise:

Let X be a r.v. with probability density function given by

$$f(x, \theta) = \begin{cases} \frac{2\theta^2}{x^3} & \text{for } x \geq \theta, \theta > 0; \\ 0 & \text{otherwise,} \end{cases}$$

and it is known that the mean of X is $m = 2\theta$.

We wish to estimate the parameter θ and, in order to do so, a random sample of size n , X_1, X_2, \dots, X_n , has been taken.

2. The method of moments estimator of θ , $\hat{\theta}_{MM}$, is:

- (A) $\frac{\bar{X}}{2}$ (B) $\frac{2}{\bar{X}}$ (C) $\frac{1}{\bar{X}}$ (D) $\frac{4}{\bar{X}}$ (E) \bar{X}

3. Is $\hat{\theta}_{MM}$ an unbiased estimator of θ ?

- (A) - (B) - (C) Yes (D) - (E) No

4. The maximum likelihood estimator of θ , $\hat{\theta}_{ML}$, is:

- (A) \bar{X} (B) $2\bar{X}$ (C) $\frac{\bar{X}}{2}$ (D) $\min(X_i)$ (E) $\frac{1}{\bar{X}}$

Questions 5 and 6 refer to the following exercise:

Let X be a r.v. with probability mass function given by:

$$P(X = -1) = \frac{\theta}{2} \quad P(X = 0) = \theta \quad P(X = 2) = 1 - \frac{3\theta}{2}$$

In order to estimate the parameter θ , a random sample of size $n = 10$ has been taken, providing the following results: -1, -1, 0, 0, 0, 0, 2, 2, 2, 2.

5. The method of moments estimate of θ is:

- (A) 0.6 (B) 0.2 (C) 0.4 (D) 0.8 (E) 1

6. The maximum likelihood estimate of θ is:

- (A) 0.4 (B) 0.2 (C) 1 (D) 0.8 (E) 0.6

Questions 7 and 8 refer to the following exercise:

We have a r.s. of size n taken from a Poisson distribution of parameter λ . In order to estimate λ , we use the estimator $\hat{\lambda} = \bar{X} + \frac{1}{n^2}$.

7. This estimator of λ is:

- (A) biased and asymptotically biased
- (B) unbiased and asymptotically unbiased
- (C) biased and asymptotically unbiased
- (D) unbiased and asymptotically biased
- (E) All false

8. Is this a consistent estimator of λ ?

- (A) Yes (B) - (C) - (D) - (E) No

Questions 9 and 10 refer to the following exercise:

Let X_1, \dots, X_n be a r.s. taken from a $U[0, \theta + 2]$ population (having a uniform distribution between 0 and $\theta + 2$) with mean $m = (\theta + 2)/2$ and variance $\sigma^2 = (\theta + 2)^2/12$. If we define the estimators

$$\hat{\theta}_1 = 2\bar{X} - 2$$

$$\hat{\theta}_2 = \frac{X_1 + 2X_2 + 2X_3 + \dots + 2X_{n-2} + 2X_{n-1} + X_n}{(n-1)} - 2$$

9. We have that:

- (A) Only $\hat{\theta}_1$ is unbiased
- (B) Both estimators are biased
- (C) Only $\hat{\theta}_2$ is unbiased
- (D) Both estimators are unbiased
- (E) It cannot be determined from the information provided

10. We have that:

- (A) -
- (B) Only $\hat{\theta}_2$ is consistent
- (C) Only $\hat{\theta}_1$ is consistent
- (D) Both estimators are consistent
- (E) It cannot be determined from the information provided

11. Let X be a random variable with probability density function given by:

$$f(x, \theta) = \frac{2}{\theta^2} x e^{-\frac{x^2}{\theta^2}} \quad x > 0, \quad \theta > 0$$

In order to test the null hypothesis $\theta = 2$ against the alternative $\theta = 4$, we take a random sample of size $n = 1$. The most powerful critical region for this observation and for a given significance level is of the form:

- (A) $X \in (C_1, C_2)$ (B) $X \in (C_1, C_2)^c$ (C) $X \leq C$ (D) $X \geq C$ (E) -

Questions 12 and 13 refer to the following exercise:

Let X be a random variable with probability mass function given by:

$$P(X = -2) = 2\theta \quad P(X = 0) = \theta \quad P(X = 2) = 1 - 3\theta$$

In order to test the null hypothesis $\theta = 0.1$ against the alternative $\theta = 0.3$, we take a random sample of size $n = 1$ and decide to reject the null hypothesis if X equals -2 or 0.

12. The significance level for this test is:

- (A) 0.3 (B) 0.9 (C) All false (D) 0.1 (E) 0.7

13. The probability of type II error for this test is:

- (A) 0.7 (B) 0.9 (C) 0.3 (D) 0.1 (E) All false

14. Let X be a r.v. having a Poisson distribution with parameter λ . We wish to test the null hypothesis $\lambda = 1$ against the alternative $\lambda = 0.5$. In order to do this, a random sample of size $n = 8$ has been taken and we decide to reject the null hypothesis if $X_1 + X_2 + \cdots + X_8 \leq 3$. The power for this statistical test is:

- (A) 0.238 (B) 0.567 (C) 0.195 (D) 0.762 (E) 0.433